

B.Sc. Semester - 5 (NEP-2020) Examination

Oct/Nov - 2025

MATH: Fundamentals of Partial Differential Calculus
(For Chemistry & Physics Students) (Minor-5)

Time: 2:00 Hours

Marks: 50

Instructions:

1. All questions are compulsory.
2. Figures to the right indicate marks.

Que.1 Answer any two out of three. (10)

- (1) State and prove Euler's theorem for Homogeneous function of two variables.

From this theorem deduce that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = n \frac{f(u)}{f'(u)}$, Where Z is a homogeneous

Function of x and y of degree n and $Z = f(u)$.

- (2) if $f(x,y) = 0$ then find formula of $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$.

- (3) if $u = \sin^{-1}(x-y)$, $x = 3t$, $y = 4t^3$ then find $\frac{du}{dt}$.

Que.2 Answer any two out of three. (10)

- (1) State and prove Taylor's theorem for two variables.

- (2) Find the maximum value of $f(x,y,z)=xyz$ subject to the constraint $2x+2y+z=108$.

- (3) Find the least distance of the point on the plane $ax+by+cz+d = 0$ from the origin.

Que.3 Answer any two out of three. (10)

- (1) Derive Charpit's method for finding the complete integral of a non linear partial differential equation.

- (2) State all four standard forms of non linear partial differential equations of first order and solve: $p^2 + q^2 = x + y$.

- (3) Solve the PDE $pxy + pq + qy - yz = 0$ by Charpit's method.

Que.4 Answer any two out of three. (10)

- (1) Solve: $\frac{\partial^3 z}{\partial x^3} - 2 \frac{\partial^3 z}{\partial x^2 \partial y} = 3x^2y$.

- (2) Solve: $\frac{\partial^3 z}{\partial x^3} - 4 \frac{\partial^3 z}{\partial x^2 \partial y} + 4 \frac{\partial^3 z}{\partial x \partial y^2} = 2\sin(3x + 2y)$.

- (3) Solve: $q^2r - 2pqs + p^2t = 0$.

Que.5 Answer any two out of three. (10)

- (1) if $z^3 - xz - y = 0$ then find $\frac{\partial^2 z}{\partial x \partial y}$.

- (2) if $u = \frac{yz}{x}$, $v = \frac{zx}{y}$, $w = \frac{xy}{z}$, then find $\frac{\partial(u,v,w)}{\partial(x,y,z)}$.

- (3) Solve: Lagrange's Linear equation $(y + z)p - (z + x)q = (x - y)$.
